



POWER ELECTRONICS I

AC-DC Converters

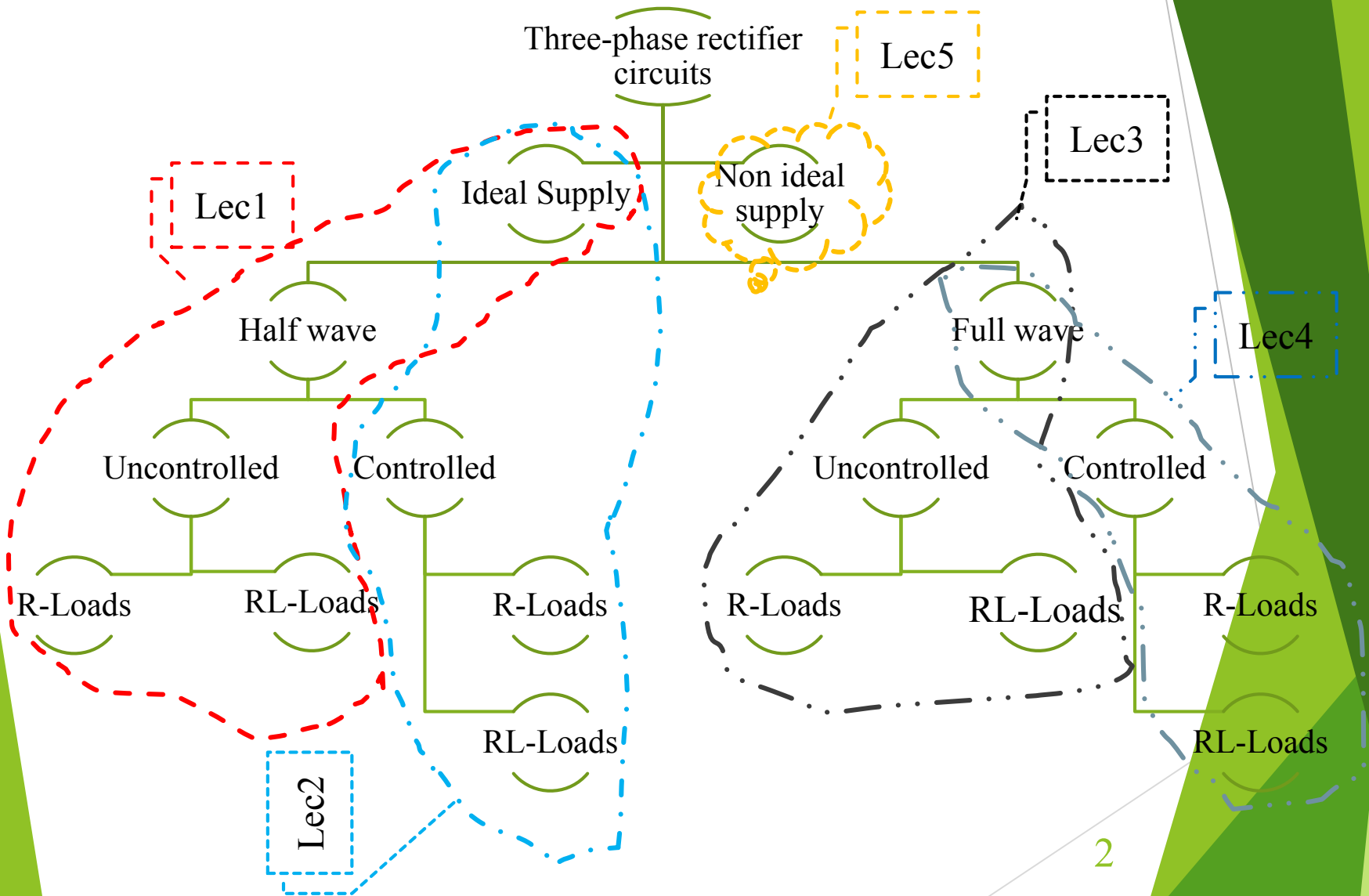
Three-Phase Rectifiers

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Three-phase rectifier Plan



Lec (6): Control of DC Motor and Open discussion

Lecture one: Three-phase half-wave uncontrolled rectifiers

Introduction

- Advantages
- Disadvantages
- Types in industry

Construction

- Circuit diagram
- Components

Operation

- Three-phase supply (phase voltage)
- Output waveforms

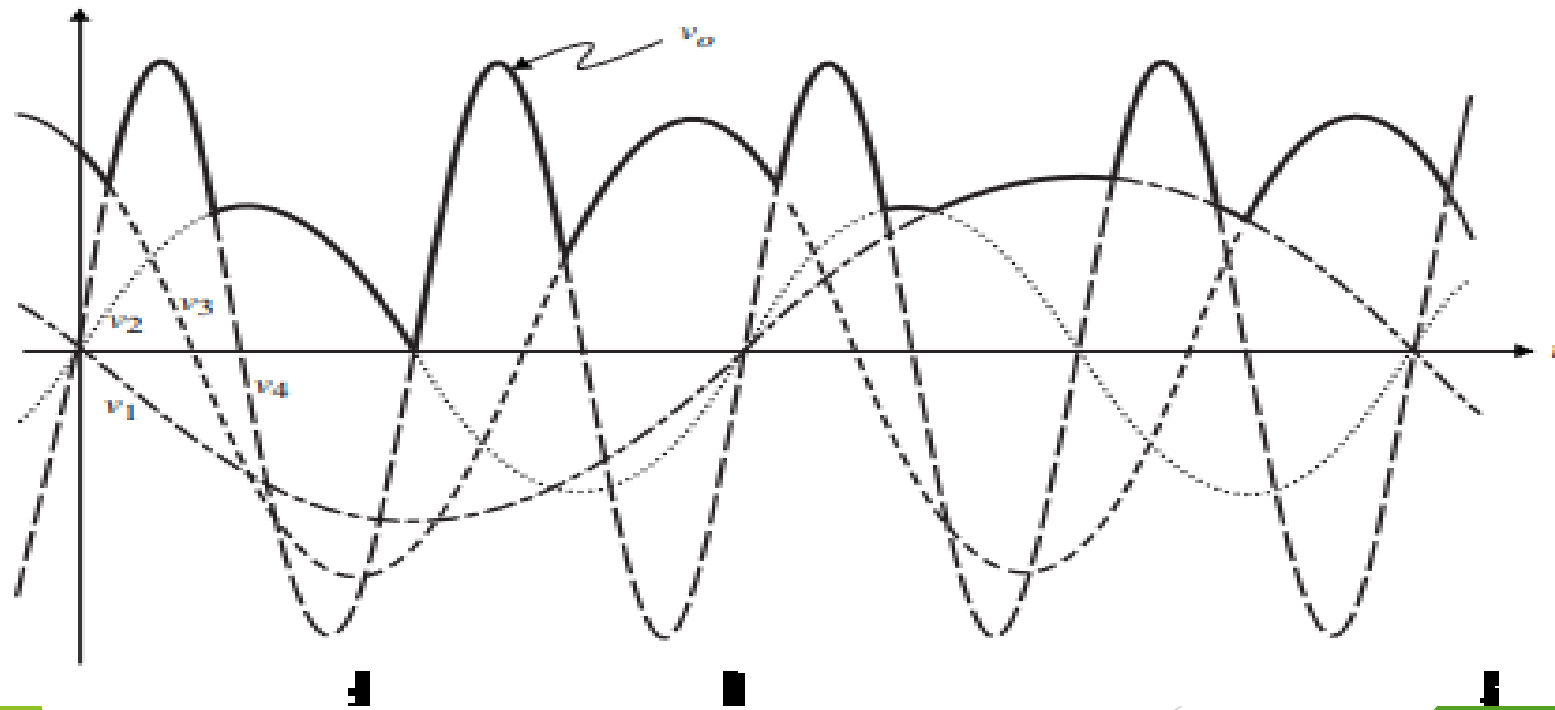
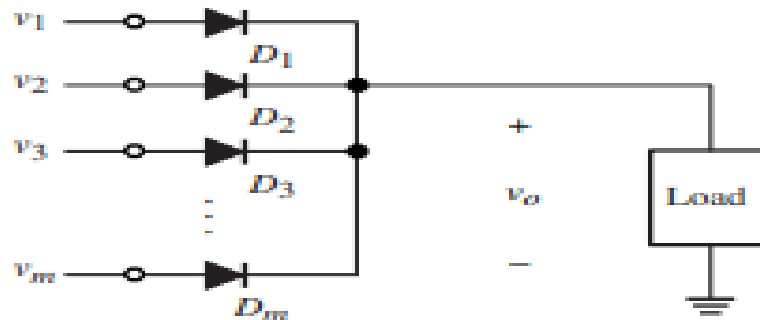
Analysis

- Analysis of the circuit with R-load
- Analysis of the circuit with highly inductive load

End

- Summery
- Questions

Main idea: Random m-phase sinusoidal input



Introduction

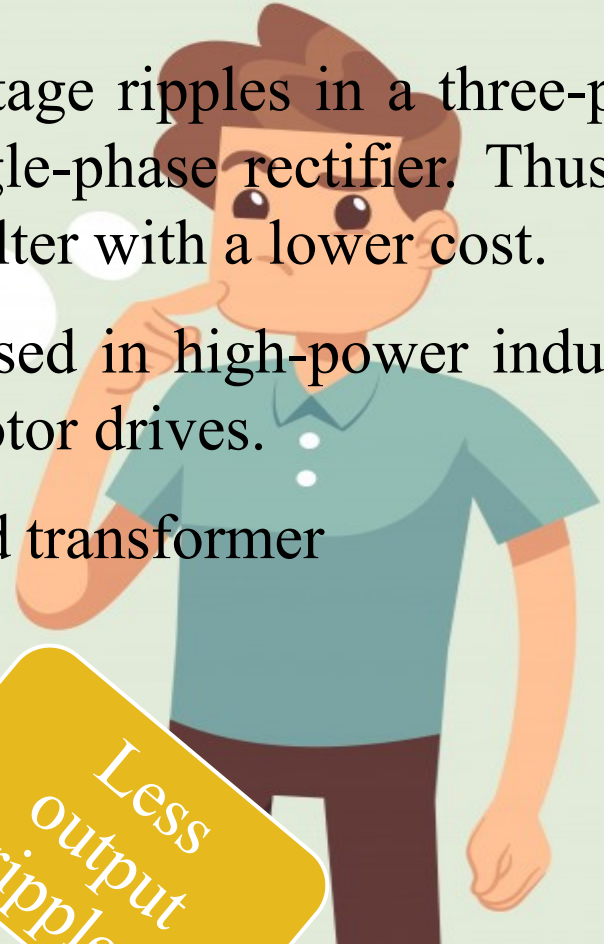
Why three-phase rectifiers ?

- Three-phase rectifiers provide higher average output voltage compared to the single-phase rectifier.
- The harmonics frequency of output voltage ripples in a three-phase rectifier is higher compared to the single-phase rectifier. Thus, the three-phase rectifier requires a smaller filter with a lower cost.
- Three-phase rectifiers are extensively used in high-power industrial applications including variable-speed motor drives.
- It doesn't require a special center-tapped transformer

High
efficiency

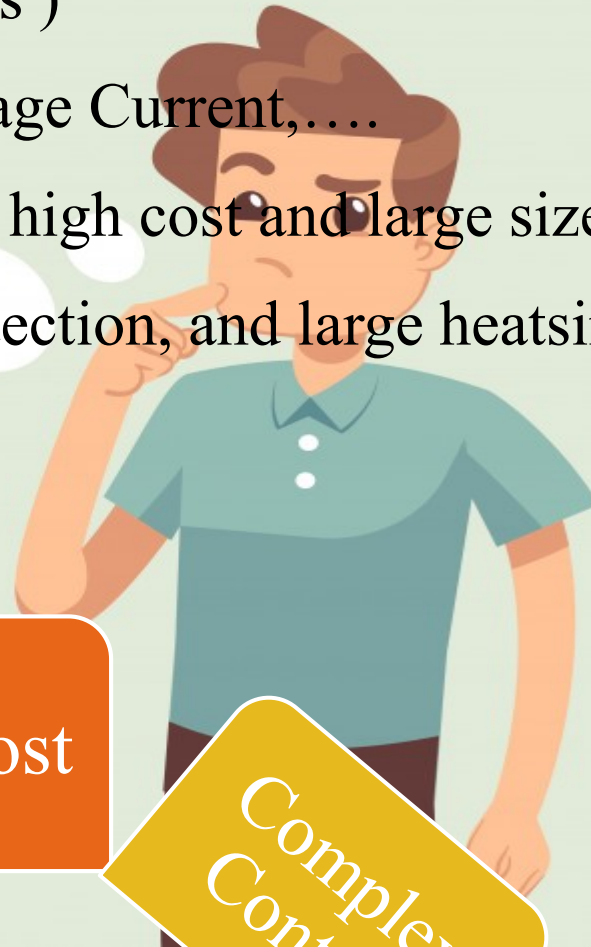
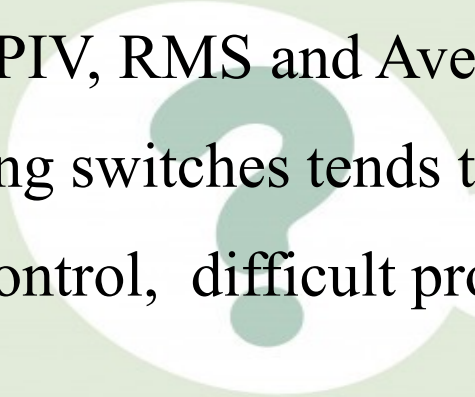
Large DC
output

Less
output
ripples



Disadvantages:

- Three-phase rectifiers require **higher rating** of the power electronics switches (Diodes and Thyristors)
 - ✓ PIV, RMS and Average Current,....
- Higher rating switches tends to high cost and large size.
- Complex control, difficult protection, and large heatsink,



High Cost

High Switch
Rating

Complex
Control

Types in Industry

- 35 A , 1000V Three Phase Bridge Rectifier: (2.63\$)
 - ✓ work on all battery banks.
 - ✓ work on all AC generators that produce 35 Amps or less
- 200 A 1600V Diode Bridge Rectifier:
 - ✓ High Power Rectifier Silicon Full Wave Diode Bridge Rectifier
 - ✓ Wind turbine with permanent magnet synchronous generator.



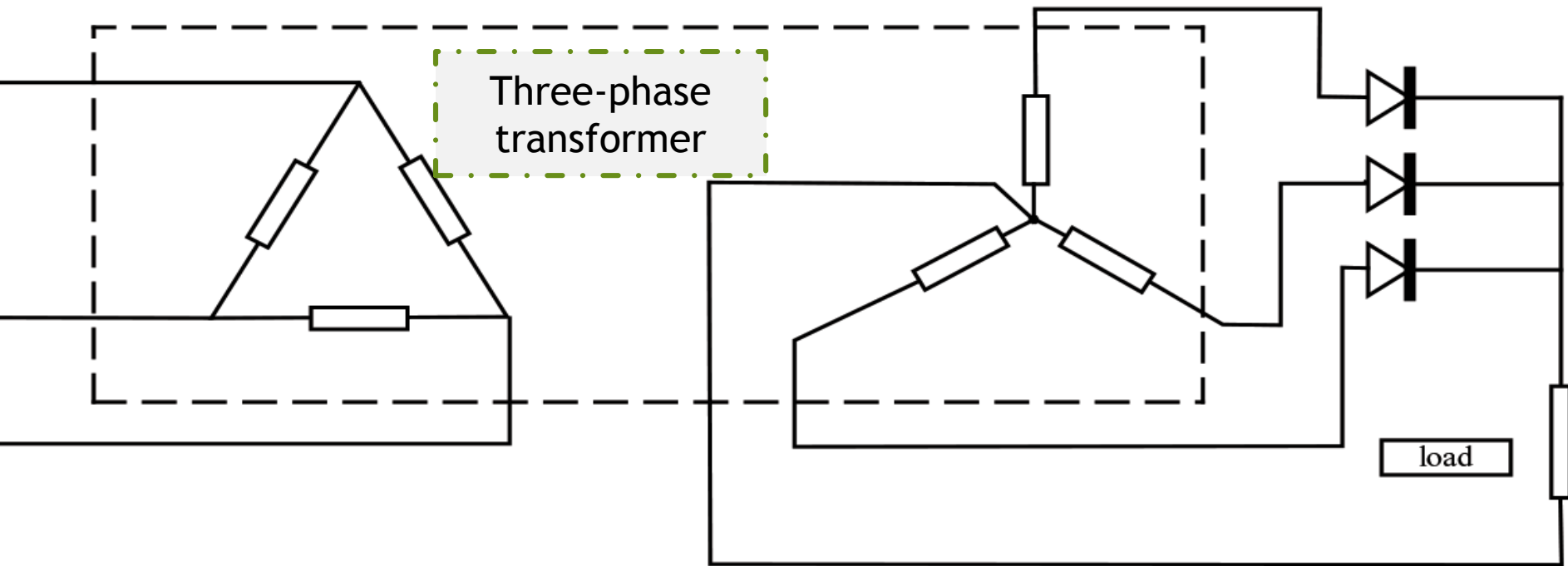
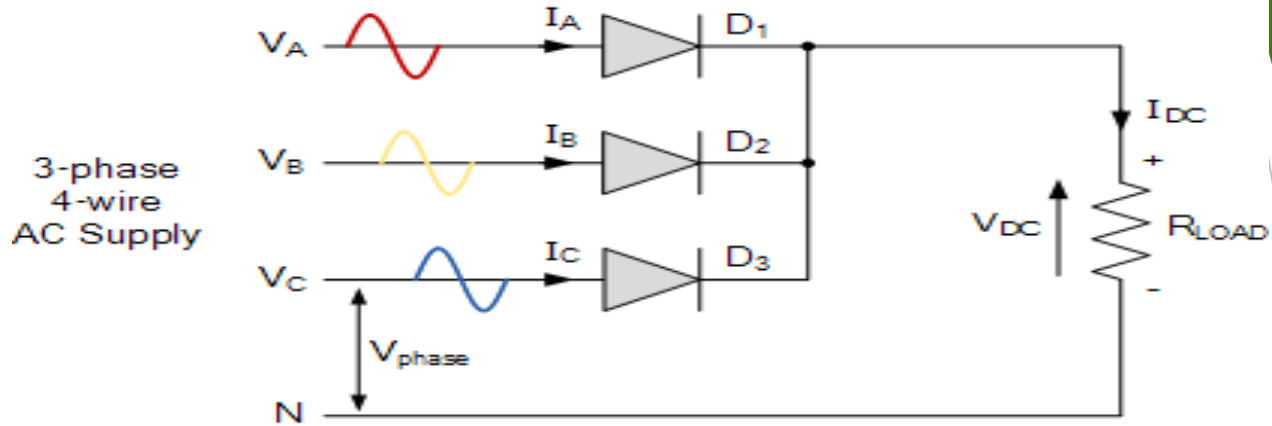
Types in Industry

Maximum Ratings ($T_a=25^\circ\text{C}$ Unless otherwise specified)

PARAMETER	SYMBOL	UNIT	SKBPC3504	SKBPC3506	SKBPC3508	SKBPC3510	SKBPC3512	SKBPC3514	SKBPC3516
Device marking code			SKBPC3504	SKBPC3506	SKBPC3508	SKBPC3510	SKBPC3512	SKBPC3514	SKBPC3516
Repetitive Peak Reverse Voltage	VRRM	V	400	600	800	1000	1200	1400	1600
Average Rectified Output Current @60Hz sine wave, R-load, With heatsink $T_c=55^\circ\text{C}$	I_O	A	35						
Surge(Non-repetitive)Forward Current @60HZ Half- sine Wave, 1 cycle, $T_a=25^\circ\text{C}$	I_{FSM}	A	400						
Current Squared Time @1msst<8.3ms $T_j=25^\circ\text{C}$, Rating of per diode	I^2t	A^2S	664						
Storage Temperature	T_{stg}	$^\circ\text{C}$	-55 ~+150						
Junction Temperature	T_j	$^\circ\text{C}$	-55 ~+150						

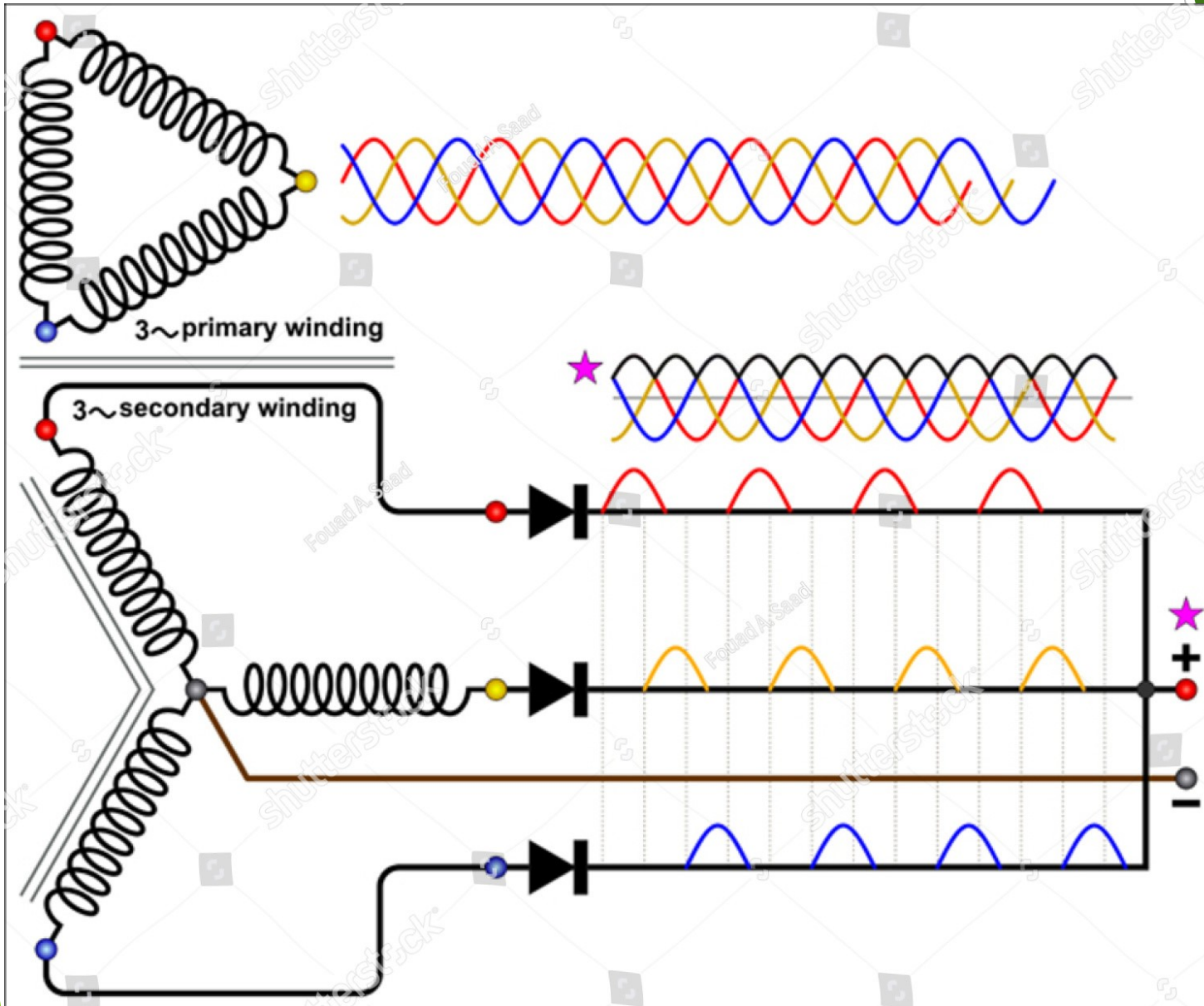
Construction

Power circuit and its components



Operation

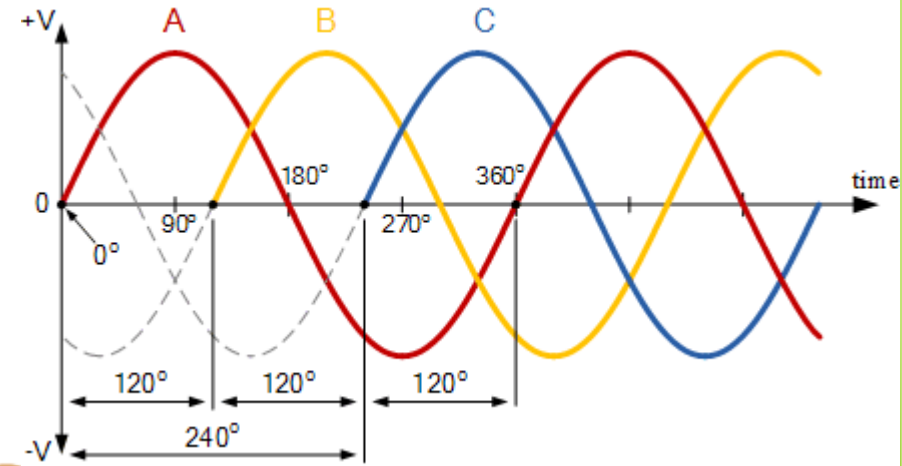
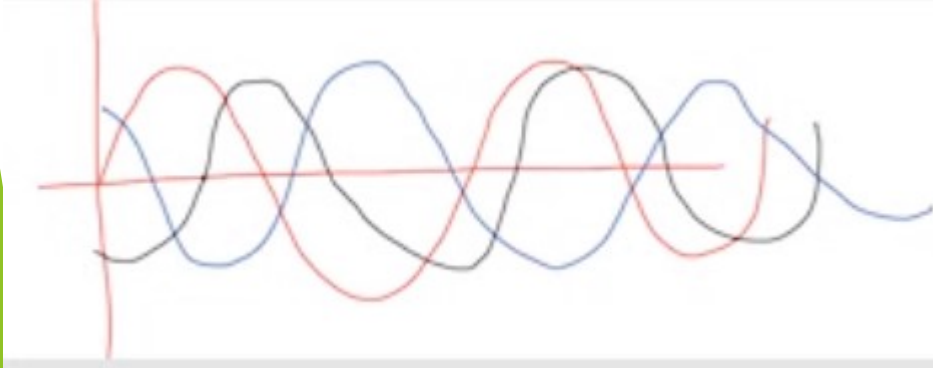
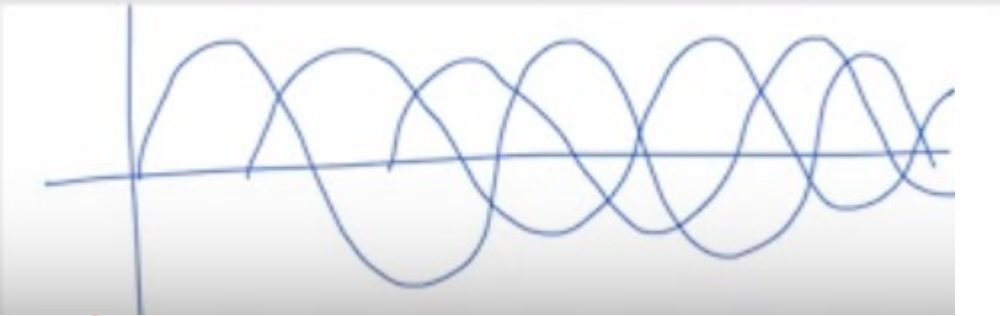
Output voltage



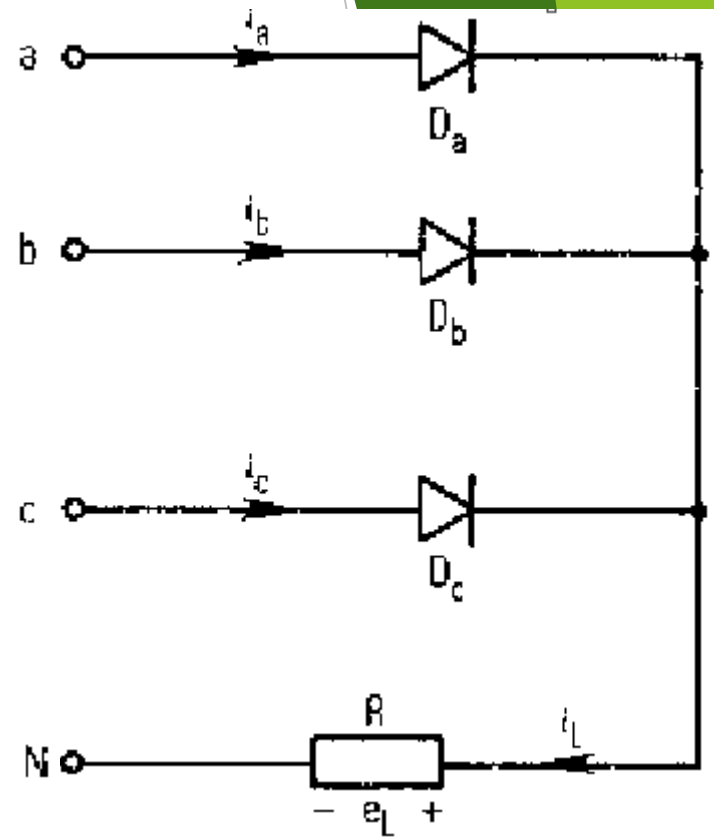
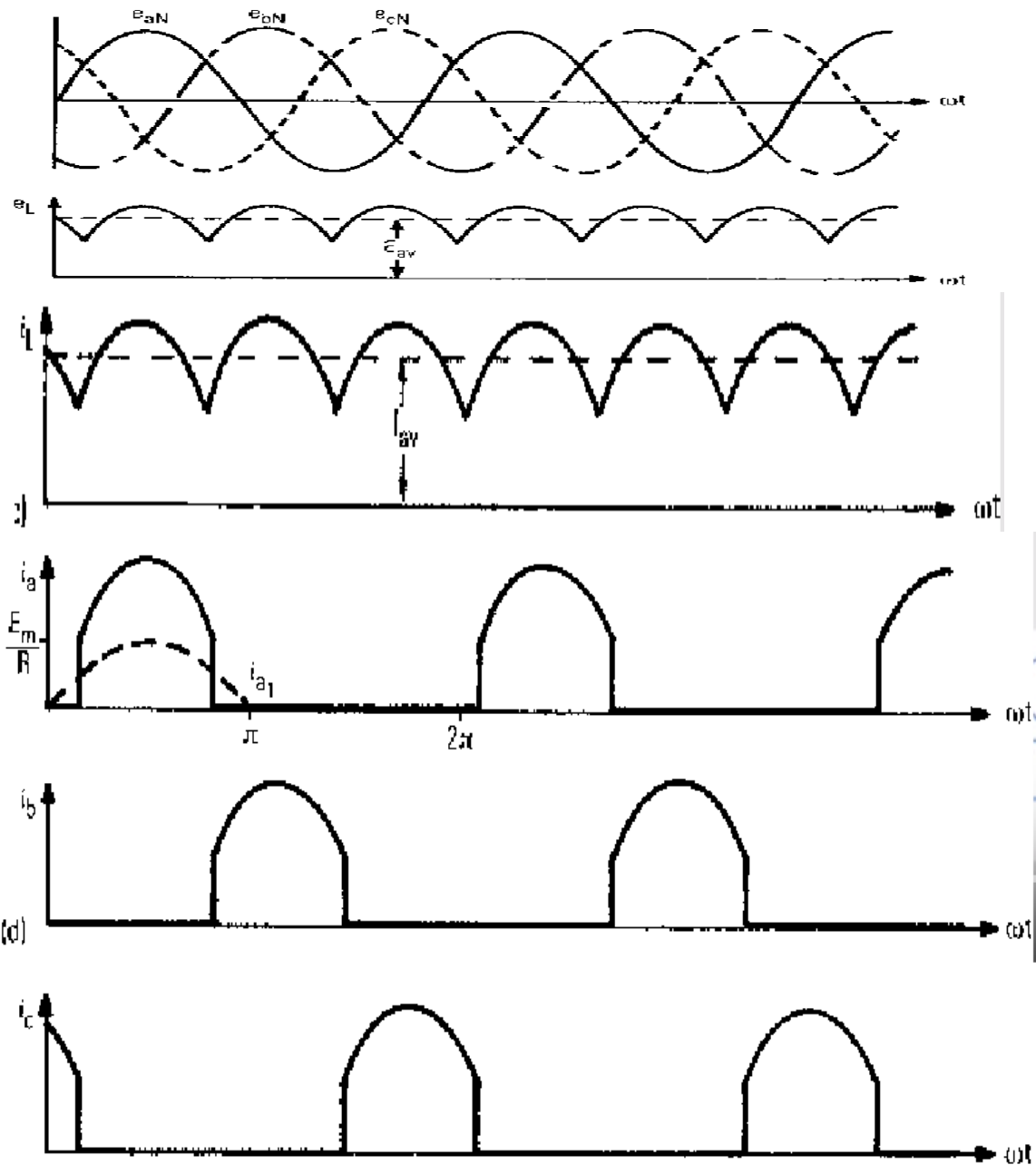
Operation

Draw three-phase waveforms

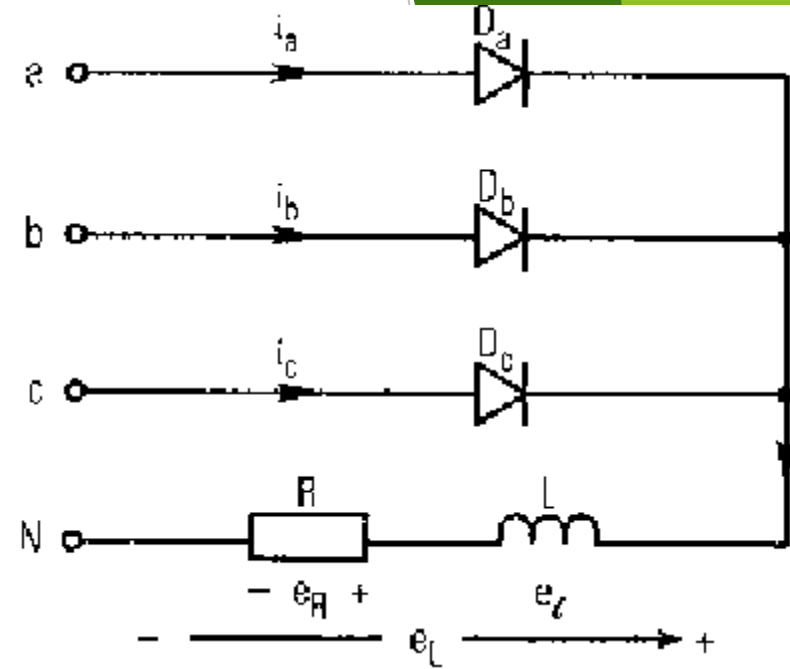
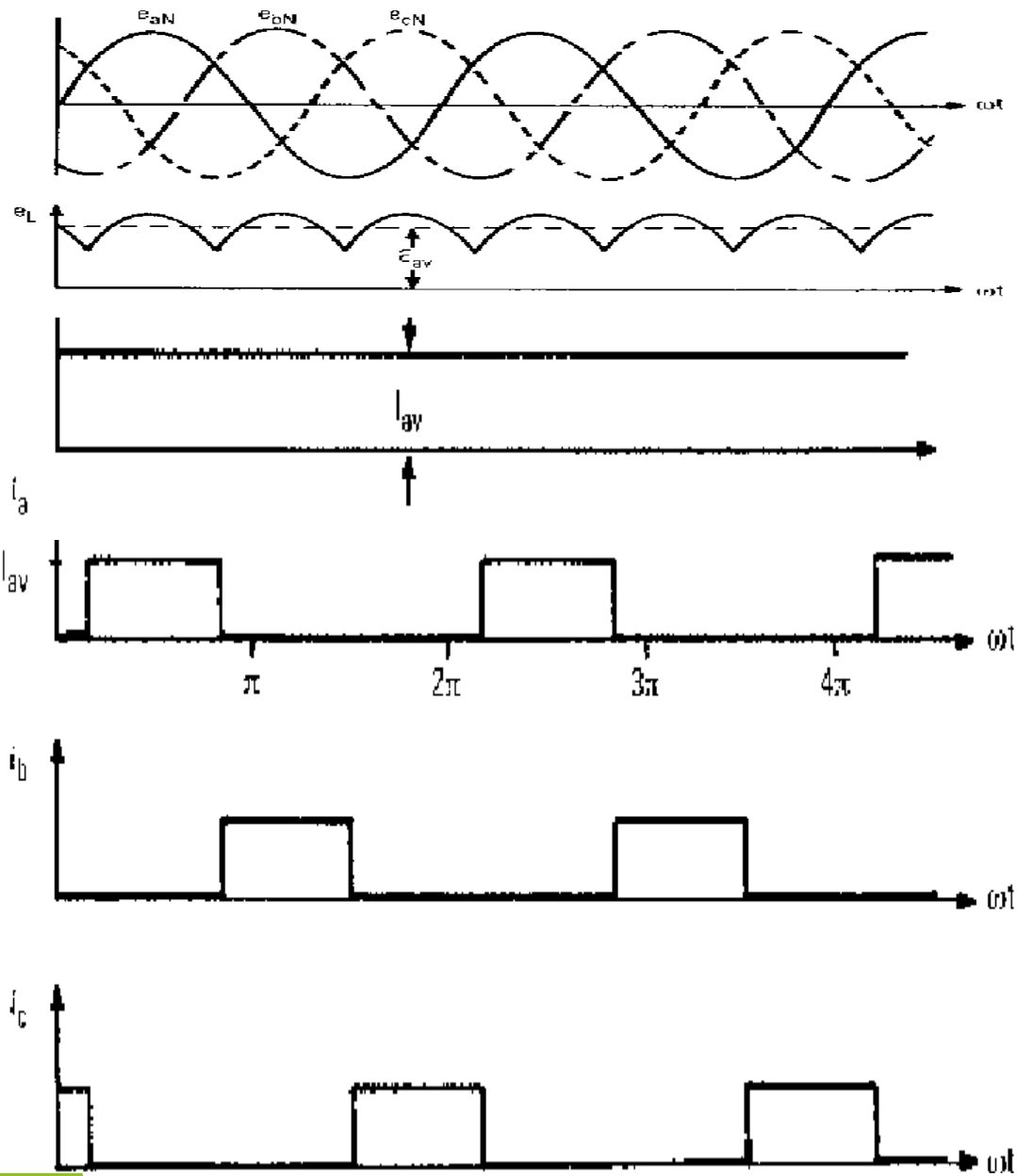
Drawing of some students :



Operation: Resistive Loads



Operation: Highly Inductive Loads



Analysis: Resistive Loads

1- Supply voltages:

$$V_a(\omega t) = V_m \sin(\omega t),$$

$$V_b(\omega t) = V_m \sin(\omega t - 2\pi/3)$$

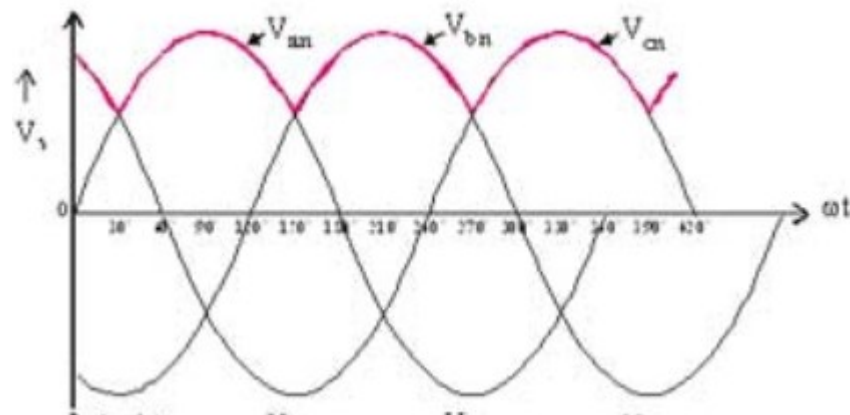
$$V_c(\omega t) = V_m \sin(\omega t - 4\pi/3)$$

2- Average Load Voltage

$$V_{o,avg} = \frac{3}{2\pi} \int_{\pi/6}^{5\pi/6} V_a(\omega t) d\omega t$$

$$= \frac{3}{2\pi} \int_{5\pi/6}^{3\pi/2} V_b(\omega t) d\omega t$$

$$= \frac{3}{2\pi} \int_{3\pi/2}^{13\pi/6} V_c(\omega t) d\omega t$$



$$V_{o,avg} = \frac{3\sqrt{3}V_m}{2\pi}$$

$$V_{o,avg} = \frac{3\sqrt{6}V_s}{2\pi}$$

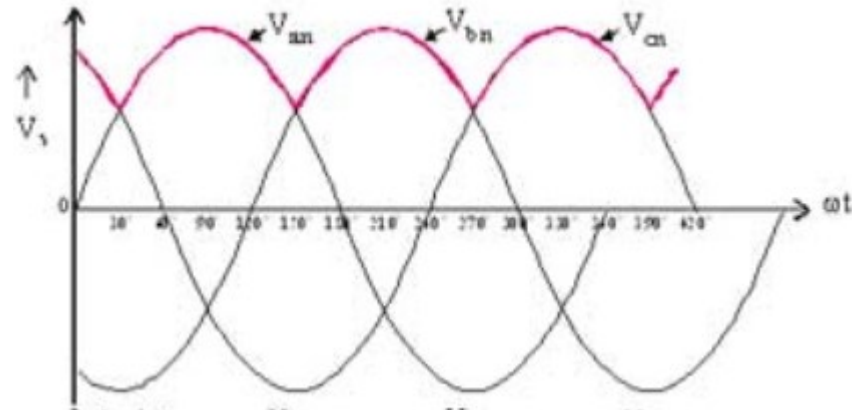
$$V_{o,avg} = 1.169V_s$$

Comment!

Analysis: Resistive Loads

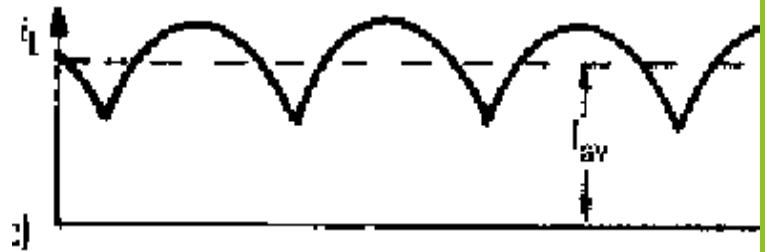
3- RMS Load voltage

$$V_{o,rms} = \left[\frac{3}{2\pi} \int_{\pi/6}^{5\pi/6} 2V_s^2 \sin^2 \omega t \, d(\omega t) \right]^{\frac{1}{2}}$$
$$= \left[1 + \frac{3\sqrt{3}}{4\pi} \right]^{\frac{1}{2}} V_s$$



4- Average load current

$$I_{o,avg} = \frac{V_{o,avg}}{R} = \frac{3\sqrt{3}V_m}{2\pi R}$$



5- RMS Load current

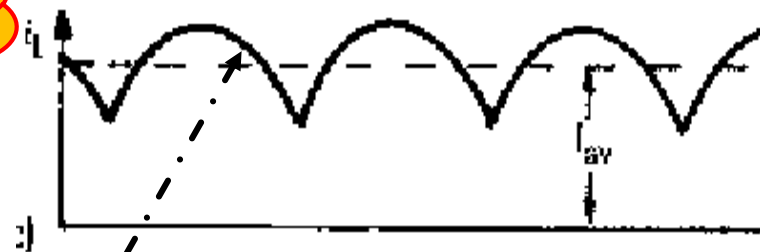
$$I_{o,rms} = V_{o,rms} / R$$

Analysis: Resistive Loads

6- Average Supply currents

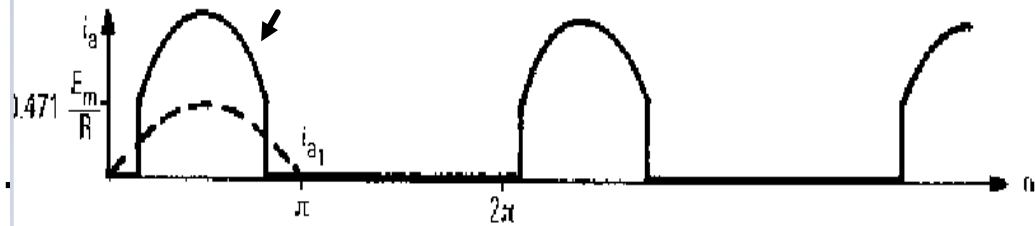
Comment!

$$I_{a, avg} = I_{b, avg} = I_{c, avg} = \frac{I_{o, avg}}{3}$$



7- RMS supply current

$$I_{s, rms} = \frac{I_{o, rms}}{\sqrt{3}}$$



8- Output power

Comment!

$$P_s = P_o = I_{o, rms}^2 R$$



9- Input power factor

$$pf = \frac{P_o}{S} = \frac{I_{o, rms}^2 R}{3V_s I_{o, rms} / \sqrt{3}}$$



Analysis: Highly Inductive Loads

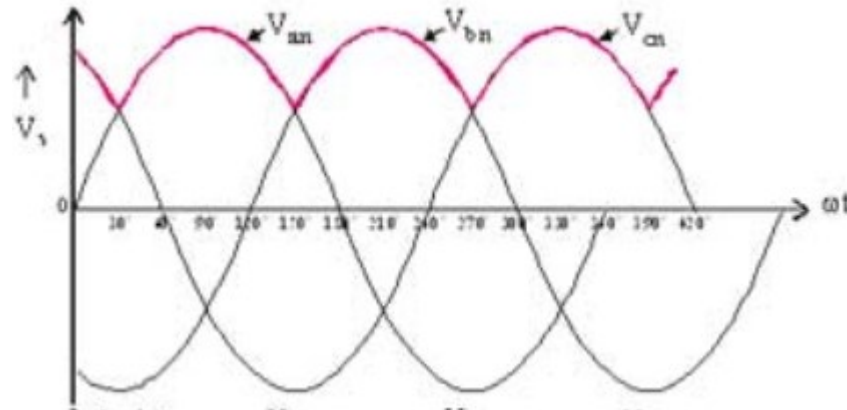
1- Average Load Voltage

$$V_{o, avg} = \frac{3\sqrt{3}V_m}{2\pi}$$

$$V_{o, avg} = \frac{3\sqrt{6}V_s}{2\pi}$$

$$V_{o, avg} = 1.169V_s$$

Comment!

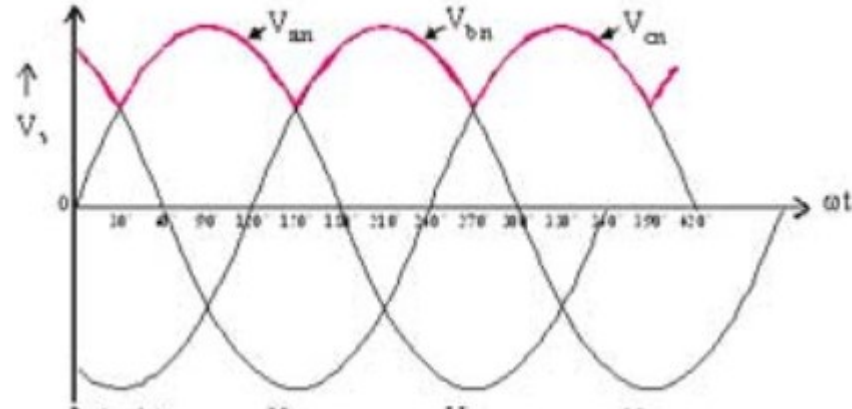


Analysis: Highly Inductive Loads

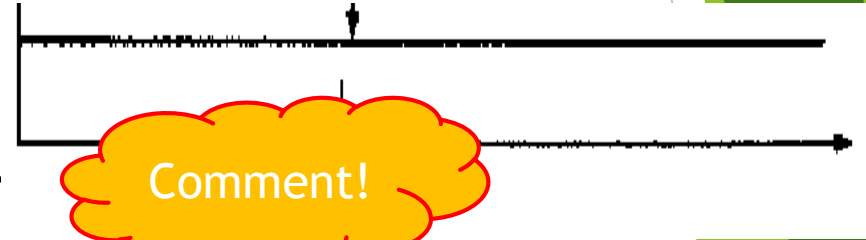
2- RMS Load voltage

$$V_{o,rms} = \left[\frac{3}{2\pi} \int_{\pi/6}^{5\pi/6} 2V_s^2 \sin^2 \omega t \, d(\omega t) \right]^{1/2}$$

$$= \left[1 + \frac{3\sqrt{3}}{4\pi} \right]^{1/2} V_s$$



3- Average load current



$$I_{o,avg} = \frac{V_{o,avg}}{R} = \frac{3\sqrt{3}V_m}{2\pi R}$$



4- RMS Load current

$$I_{o,rms} = I_{o,avg}$$

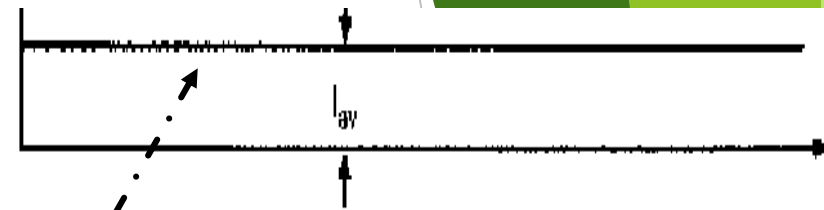
Converter efficiency:

$$\eta = \frac{P_{dc}}{P_{o,rms}} = \frac{V_{o,avg} I_{o,avg}}{V_{o,rms} I_{o,rms}}$$

Analysis: Highly Inductive Loads

5- Average Supply currents

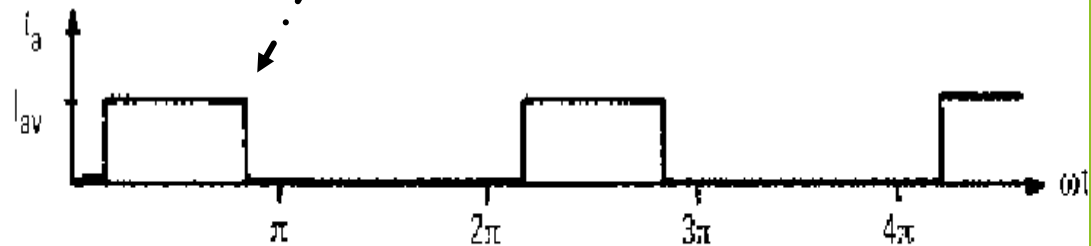
$$I_{a, avg} = I_{b, avg} = I_{c, avg} = \frac{I_{o, avg}}{3}$$



6- RMS supply current

$$I_{s, rms} = \frac{I_{o, avg}}{\sqrt{3}}$$

Comment!



7- Output power

$$P_s = P_o = I_{o, avg}^2 R$$



8- Input power factor

$$pf = \frac{P_o}{S} = \frac{I_{o, avg}^2 R}{3V_s I_{o, avg} / \sqrt{3}}$$



Summery

	R-Load	Highly inductive load
$V_{o,avg}$	The same waveforms so the same average values $\boxed{V_{o,avg} = \frac{3\sqrt{3}V_m}{2\pi}}$	
$V_{o,rms}$	$= \left[1 + \frac{3\sqrt{3}}{4\pi} \right]^{\frac{1}{2}} V_S$	
$I_{o,avg}$	$\boxed{I_{o,avg} = \frac{V_{o,avg}}{R} = \frac{3\sqrt{3}V_m}{2\pi R}}$	
$I_{o,rms}$	$V_{o,rms}/R$	$I_{o,avg}$
$I_{s,avg}$	$I_{o,avg}/3$	
$I_{s,rms}$	$I_{o,rms}/\text{sqrt}(3)$	$I_{o,avg}/\text{sqrt}(3)$

Questions

- Q₁) what are the rating values of the Diodes in the converter?
- Q₂) Draw the waveforms of the diodes voltage and current
- Q₃) Compare between the rms harmonic voltages in single phase and three phase half wave uncontrolled rectifiers
- Q₄) what are the disadvantages of the three-phase half –wave rectifiers?
- Q₅) Do you need to use a freewheeling diode in the pervious circuit?
- Q₆) Write an expression for the instantaneous load current for all pervious case studies